# Territorial control in civil wars: Theory and measurement using machine learning

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#### New Faces in Political Methodology XI, Penn State University

#### Symmetric conflict - Ukraine



#### Symmetric conflict - Ukraine



#### Asymmetric conflict - Nigeria



#### Question

How can we measure changes in territorial control across space and time?



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#### Argument

We can estimate territorial control leveraging variation rebel tactics.



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#### Contribution

- Measurement model for rebel tactics.
- Hidden Markov Model (HMM) estimates of territorial control.

#### Model of territorial control & rebel tactics

# Model of territorial control & rebel tacticsMeasuring conflict exposure

- Model of territorial control & rebel tactics
- Measuring conflict exposure
- Hidden Markov Model (HMM)

- Model of territorial control & rebel tactics
- Measuring conflict exposure
- Hidden Markov Model (HMM)
- HMM estimates & validation
  - Nigeria
  - Colombia

#### Territorial control influences tactical choices in civil wars. [Carter 2015, de la Calle and Sánchez-Cuenca 2015, 2012]

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#### Higher rebel control

#### $\implies$ Conventional tactics



Higher rebel control

 $\implies$  Conventional tactics



#### Lower rebel control

#### $\implies$ Terrorist attacks



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## Co-occurrence of conventional and terrorist tactics

Event locations in Nigeria 2014



## Co-occurrence of conventional and terrorist tactics



## VCo-occurrence of conventional and terrorist tactics

Event locations in Nigeria 2014



## Co-occurrence of conventional and terrorist tactics

Event locations in Nigeria 2014



## Continuum of territorial control



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$$egin{array}{l} {\it Tactics}_{it} = \{{\sf A}, {\sf B}, {\sf C}, {\sf D}\} \ = f\left({\sf E}_{it}^{[{\it T}]}, {\sf E}_{it}^{[{\it C}]}
ight) \end{array}$$

 $E_{it}^{[T]}$  area *i*'s exposure to terrorist events at *t*  $E_{it}^{[C]}$  area *i*'s exposure to conventional events at *t* 





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Unit of observation: cell-month  $C_{it}$ 



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a) Spatial distance  $d_{ij}$  in km, temporal distance (age)  $a_{jt}$  in months.



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b) Logistic weights  $w_{d_{ii}}$  and  $w_{a_{it}}$ 

$$w_{d_{ij}} = rac{1}{1+e^{-7+0.35d_{ij}}} \ w_{a_{jt}} = rac{1}{1+e^{-8+2.5a_{jt}}}$$



Unit of observation: cell-month  $C_{it}$ 

a) Spatial distance  $d_{ij}$  in km, temporal distance (age)  $a_{jt}$  in months.

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$$w_{d_{ij}} = rac{1}{1+e^{-7+0.35d_{ij}}} \ w_{a_{jt}} = rac{1}{1+e^{-8+2.5a_{jt}}}$$

c) Exposure E

$$E_{it} = \sum_{j=1}^{J} \left( w_{d_{ij}} \times w_{a_{tm}} 
ight)$$



#### Logistic decay functions

$$f(d) = \frac{1}{1 + e^{-\kappa + \lambda d}}$$



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#### **Continuous** assignment





#### **Continuous** assignment



Reduce MAUP



#### **Continuous** assignment



- Reduce MAUP
- Spatial dependency in HMM

#### Hidden Markov Model



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## Hidden Markov Model



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## Hidden Markov Model



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## HMM estimates for Nigeria



[Discrete monthly-level estimates averaged for each year, N = 942]

## HMM estimates for Nigeria

[Discrete monthly-level estimates averaged for each year, N = 942]

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## Validation

#### HMM estimates



#### ACLED validation data



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## Validation

#### HMM estimates



#### ACLED validation data





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## HMM estimates for Colombia

[Discrete monthly-level estimates averaged for each year,  $\mathsf{N}=\mathsf{851}]$ 

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#### HMM estimates for Colombia 2015 vs. 2015



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# Hypothesis

Rebel-controlled areas have a higher probability of deforestation post-peace than government-controlled areas.



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 $Deforest_{i,t} = \beta_0 + \beta_1 \Delta Control_{i,t} + \beta_2 Peace_t + \beta_3 (\Delta Control_{i,t} \times Peace_t) + \epsilon_i$ 

 $\begin{aligned} & \text{Deforest}_{i,t} \text{ Deforestation in grid cell (0/1, from IDEAM)} \\ & \text{Control}_{i,t} \text{ HMM Territorial control estimate (1 = gov. control)} \\ & \text{Peace}_t \text{ Peace agreement 2016 (0/1)} \end{aligned}$ 

$$N = 3,404 \ (I = 851,2013 - 2016)$$



DV: Deforestation dummy

[Bootstrapped standard errors clustered by grid cell.]

## Discussion

HMMs are promising method to estimate territorial control.



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# Appendix

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## Hidden Markov Random Field (HMRF) model



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## Picture sources (in the order they appear)

#### Risk board game

https://www.flickr.com/photos/tambako/4598642399, licensed under CC BY-ND 2.0, accessed 16 July 2016.

- Nigeria map https://reliefweb.int/sites/reliefweb. int/files/resources/Nigeria\_Boko\_Haram\_threat\_ dec%202015.pdf.
- Ukraine http://www.kas.de/wf/en/33.48639/.
- Oeforestation https:

//www.flickr.com/photos/16725630@N00/1524189000/.

Most probable path for hidden state  $q_h$  at t:

$$v_t(h) = \max_{g=1}^N v_{t-1}(g)\theta_{gh}\phi_h(o_t)$$

[Maximum likelihood sequence of labels via argmax]

 $h \dots$  indexes current state  $g \dots$  indexed previous state  $v_{t-1}(g) \dots$  path probability of previous time step  $\theta_{gh} \dots$  transition probability from  $q_g$  to  $q_h$   $\phi_h(o_t) \dots$  emission probability given h HMM returns path labels for maximum likelihood of observation sequence.

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| Observation                                                                                                    | Latent variable                                |
|----------------------------------------------------------------------------------------------------------------|------------------------------------------------|
| $\overline{E_{it}^{[T]} \approx E_{it}^{[C]} \approx 0}$ $C_{it} > T_{it}, \text{ and }  C_{it} - T_{it}  > m$ | Full rebel control<br>Incomplete rebel control |
| $ C_{it} - T_{it}  < m$                                                                                        | Highly contested                               |
| $C_{it} < T_{it}$ , and $ C_{it} - T_{it}  > m$                                                                | Incomplete government control                  |
| $E_{it}^{[T]} pprox E_{it}^{[C]} pprox 0$                                                                      | Full government control                        |

- m = 0.025
- *T<sub>it</sub>* = *P*([*E<sub>it</sub><sup>[T]</sup>*]; λ<sub>t</sub><sup>[T]</sup>) and *C<sub>it</sub>* = *P*([*E<sub>it</sub><sup>[C]</sup>*]; λ<sub>t</sub><sup>[C]</sup>) are probabilities from a zero-inflated Poisson distribution.
- λ<sub>t</sub><sup>[T]</sup> and λ<sub>t</sub><sup>[C]</sup> denote expected number of events for each tactic in a given time period t across all areas I within a country.

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## Resampling grid cell locations



 $C_1$  1T, 0C: Tactics<sub>it</sub> = D  $C_2$  5T, 4C: Tactics<sub>it</sub> = D  $C_3$  0T, 0C: Tactics<sub>it</sub> = A



#### Spatial decay functions

Sample parameter values for spatial logistic decay function



λ - 0.1 - 0.5 - 2.5 - 5 - 7.5

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#### Temporal decay functions

Sample parameter values for temporal logistic decay function



λ - 1 - 2.5 - 5 - - 7.5 - 10

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For each grid cell

- Compute terrorist exposure E<sup>[T]</sup><sub>it</sub> and conventional exposure E<sup>[C]</sup><sub>it</sub> to events K<sub>j</sub>.
  - Spatial distance  $\longrightarrow$  spatial weight  $w_{d_{ij}}$ .
  - **2** Temporal distance  $\longrightarrow$  temporal weight  $w_{a_{it}}$ .

- Sompute  $Tactics_{it} = f(E_{it}^T, E_{it}^C)$ ,  $Tactics_{it} = \{A, B, C, D\}$ .
- Setimate  $Q = \{S1, S2, S3, S4, S5\}$  via HMM.

Transition probabilities are inspired by Kalyvas (2006).

|    | S1                         | S2                                    | $q_{t-1}$ S3                                                     | S4                                                                                                                                                                                                                                                                                                                                     | S5                                                                                                                                                                                                                                                                                                                                                                                                                                                                        |
|----|----------------------------|---------------------------------------|------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| S1 | 0.250                      | 0.500                                 | 0.025                                                            | 0.200                                                                                                                                                                                                                                                                                                                                  | 0.025                                                                                                                                                                                                                                                                                                                                                                                                                                                                     |
| S2 | 0.250                      | 0.150                                 | 0.075                                                            | 0.500                                                                                                                                                                                                                                                                                                                                  | 0.025                                                                                                                                                                                                                                                                                                                                                                                                                                                                     |
| S3 | 0.050                      | 0.025                                 | 0.050                                                            | 0.850                                                                                                                                                                                                                                                                                                                                  | 0.025                                                                                                                                                                                                                                                                                                                                                                                                                                                                     |
| S4 | 0.025                      | 0.075                                 | 0.150                                                            | 0.125                                                                                                                                                                                                                                                                                                                                  | 0.625                                                                                                                                                                                                                                                                                                                                                                                                                                                                     |
| S5 | 0.050                      | 0.075                                 | 0.475                                                            | 0.025                                                                                                                                                                                                                                                                                                                                  | 0.375                                                                                                                                                                                                                                                                                                                                                                                                                                                                     |
|    | S1<br>S2<br>S3<br>S4<br>S5 | S1S10.250S20.250S30.050S40.025S50.050 | S1S2S10.2500.500S20.2500.150S30.0500.025S40.0250.075S50.0500.075 | S1         S2 $q_{t-1}$ S1         S2         0.025           S2         0.250         0.150         0.075           S3         0.050         0.025         0.050           S3         0.050         0.025         0.050           S4         0.025         0.075         0.150           S5         0.050         0.075         0.475 | g1         g2         gt-1<br>S3         S4           S1         0.250         0.500         0.025         0.200           S2         0.250         0.150         0.075         0.500           S3         0.050         0.025         0.050         0.500           S4         0.025         0.025         0.050         0.850           S4         0.025         0.075         0.150         0.125           S5         0.050         0.075         0.475         0.025 |

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The probability value in each cell of this matrix answers the following question: "Given that the true state of the grid cell at time t is, for example, S1, what is the probability of observing, for example, A from the data?"

|   |                  |                            | $q_t$                                            |                                                                                                                                                                                                                                                                          |                                                                                                                                                                                                                                                                                                                                                        |
|---|------------------|----------------------------|--------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
|   | S1               | S2                         | <b>S</b> 3                                       | S4                                                                                                                                                                                                                                                                       | S5                                                                                                                                                                                                                                                                                                                                                     |
| А | 0.600            | 0.050                      | 0.050                                            | 0.050                                                                                                                                                                                                                                                                    | 0.600                                                                                                                                                                                                                                                                                                                                                  |
| В | 0.175            | 0.175                      | 0.600                                            | 0.175                                                                                                                                                                                                                                                                    | 0.175                                                                                                                                                                                                                                                                                                                                                  |
| С | 0.050            | 0.175                      | 0.175                                            | 0.600                                                                                                                                                                                                                                                                    | 0.175                                                                                                                                                                                                                                                                                                                                                  |
| D | 0.175            | 0.600                      | 0.175                                            | 0.175                                                                                                                                                                                                                                                                    | 0.050                                                                                                                                                                                                                                                                                                                                                  |
|   | A<br>B<br>C<br>D | S1A0.600B0.175C0.050D0.175 | S1S2A0.6000.050B0.1750.175C0.0500.175D0.1750.600 | qt         qt           S1         S2         S3           A         0.600         0.050         0.050           B         0.175         0.175         0.600           C         0.050         0.175         0.175           D         0.175         0.600         0.175 | qt         qt         S4           S1         S2         S3         S4           A         0.600         0.050         0.050         0.050           B         0.175         0.175         0.600         0.175           C         0.050         0.175         0.175         0.600           D         0.175         0.600         0.175         0.175 |

## Three fundamental problems of HMMs

Likelihood Given transition probabilities θ and emission probabilities φ, what is the likelihood of the observation sequence O?

$$P(O) = \sum_{Q} P(O, Q) = \sum_{Q} P(O|Q)P(Q)$$

- Oecoding Given transition probabilities θ and emission probabilities φ as well as the observation sequence O, what are the most likely sequence of labels for hidden states Q?
- **Output Learning** Given the observation sequence O and the structure of the HMM, what are the best transition probabilities  $\theta$  and emission probabilities  $\phi$ ?

See Jurafsky, Daniel & James H. Martin (2017): Speech and Language Processing.

#### Why actors seek territorial control

- Collaboration of population [Arjona 2016, Kalyvas 2006]
- Extract resources

[Stewart and Liou 2017, Carter 2015]

Increase mobilization

[Stewart and Liou 2017, de la Calle and Sánchez-Cuenca 2015]

• Governance

[Stewart Forthcoming]

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#### GED

- Considering only state-based conflict (disregarding violence between NSA and violence against civilians).
- Considering only events with sufficient accuracy (levels 1-3).

#### GTD

- Excluding events that are coded as doubtterr == 1.
- Considering only events with sufficient accuracy (levels 1–3).

## Nigeria estimates



Yearly averages of monthly estimates of territorial control in NE Nigeria

## ACLED validation



Table: The unit of analysis for territorial control is annual averages of monthly-level estimates for 0.25 degree hexagonal grid cells.

| Statistic                            | Ν     | Mean   | St. Dev. | Min | Max |
|--------------------------------------|-------|--------|----------|-----|-----|
| Control <sub><i>i</i>,<i>t</i></sub> | 3,404 | 0.9783 | 0.0755   | 0   | 1   |
| $\Delta Control_{i,t}$               | 3,404 | 0.0062 | 0.0895   | -1  | 1   |
| Peacet                               | 3,404 | 0.2500 | 0.4331   | 0   | 1   |
| $Deforestation_{i,t}$                | 3,404 | 0.0496 | 0.2172   | 0   | 1   |

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